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# Anomaly in the fine-structure splitting of EPR spectra of $\mathrm{Cr}^{3+}$ centres in $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ crystals 

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#### Abstract

EPR measurements have been made at room temperature on as-grown single crystals of $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$. For crystals doped with $\mathrm{Cr}^{3+}$, signals from the $\mathrm{Cr}^{3+}$ centres with monoclinic (centre II) and orthorhombic (centre III) symmetries are observed together with ones from the uncompensated tetragonal centre (centre I). On the basis of spin-Hamiltonian separation analysis, the centre II is ascribed to a $\mathrm{Cr}^{3+}$ ion substituted for a $\mathrm{Zn}^{2+}$ site with a vacancy at its nearest $\mathrm{Tl}^{+}$site. The centre III is ascribed to $\mathrm{arr}^{3+}$ ion associated with a vacancy at the nearest $\mathrm{Zn}^{2+}$ site. Anomalies were revealed in the separated parameters $b_{2 a(1)}$ for the centres II, III and in $b_{2 a(2)}$ for the centre III, which have about double the magnitude of those in the other layered perovskite fluorides $\mathrm{Rb}_{2} \mathrm{ZnF}_{4}, \mathrm{~K}_{2} \mathrm{ZnF}_{4}$ with different monovalent cations. These anomalies may be due to some effect of the nearest and the next-nearest $\mathrm{Tl}^{+}$ions.


## 1. Introduction

$\mathrm{K}_{2} \mathrm{NiF}_{4}$-like layered perovskite crystals with space group $I 4 / \mathrm{mmm}$ are interesting because of their close relationship to $\mathrm{KNiF}_{3}$-like cubic perovskite crystals. The layered crystals may be regarded as a two-dimensional network of $\mathrm{NiF}_{6}$ octahedra sharing corners, in contrast with the three-dimensional network in the cubic perovskite structure. It is known that a $\mathrm{Cr}^{3+}$ ion in cubic perovskite crystals $\mathrm{ABF}_{3}$ substitutes for a host divalent $\mathrm{B}^{2+}$ ion. Tetragonal and trigonal $\mathrm{Cr}^{3+}$ centres of several kinds are found to be formed in these crystals [1-3], where the excess monovalent positive charge on the $\mathrm{Cr}^{3+}$ ion is locally just compensated by a $\mathrm{Li}^{+}$(the $\mathrm{Cr}^{3+}-\mathrm{Li}^{+}$ centre) at the nearest $\mathrm{B}^{2+}$ site [1] or by a vacancy (the $\mathrm{Cr}^{3+}-\mathrm{V}_{\mathrm{A}}$ centre) at the nearest $\mathrm{A}^{+}$ site [2]. In these crystals, tetragonal $\mathrm{Cr}^{3+}$ centres with vacancies at the nearest $\mathrm{B}^{2+}$ site (the $\mathrm{Cr}^{3+}-\mathrm{V}_{\mathrm{B}}$ centre) [3] are also formed, though excess positive charge on the $\mathrm{Cr}^{3+}$ ion is locally overcompensated by the $\mathrm{B}^{2+}$ vacancy.


Figure 1. Unit cells of (a) virtual cubic perovskite $\mathrm{TlZnF}_{3}$ crystal and (b) layered perovskite $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ crystal.

In the layered perovskite crystals $\mathrm{A}_{2} \mathrm{BF}_{4}, \mathrm{Cr}^{3+}$ ions substitute for $\mathrm{B}^{2+}$ ions, similarly to the case for $\mathrm{ABF}_{3}$ crystals. In $\mathrm{A}_{2} \mathrm{BF}_{4}$ crystals, EPR spectra of the $\mathrm{Cr}^{3+}-\mathrm{V}_{\mathrm{B}}$ and the $\mathrm{Cr}^{3+}-\mathrm{Li}^{+}$ centres with orthorhombic symmetry have been observed together with a spectrum of the $\mathrm{Cr}^{3+}$ ion with tetragonal symmetry without any local compensation in its immediate neighbourhood (the uncompensated centre) [4-7]. For these centres the relationships between the parameters $b_{2}^{m}(m=0,2)$ and the local environments around $\mathrm{Cr}^{3+}$ ions were deduced by separating the fine-structure terms into two uniaxial terms along the $c$-axis and along the $\mathrm{Cr}^{3+}-\mathrm{V}_{\mathrm{B}}$ (or the $\mathrm{Cr}^{3+}-\mathrm{Li}^{+}$) pair direction using the spin-Hamiltonian separation method [4-8]. The structure of the centre in $\mathrm{A}_{2} \mathrm{BF}_{4}$ crystal can be considered by comparing each separated parameter with the axial parameter for the uncompensated centre observed in the same host crystal and with that for the same kind of $\mathrm{Cr}^{3+}-\mathrm{V}_{\mathrm{B}}\left(\right.$ or $\left.\mathrm{Cr}^{3+}-\mathrm{Li}^{+}\right)$centre in $\mathrm{ABF}_{3}$ crystal.

It is well known that the structures of the compounds $\mathrm{ABF}_{3}$ are closely related to the tolerance factor $t\left(=\left(r_{\mathrm{A}}+r_{\mathrm{F}}\right) / \sqrt{2}\left(r_{\mathrm{B}}+r_{\mathrm{F}}\right)\right)$. Babel [9] reported that the cubic perovskite structure occurs in the range of the tolerance factor $0.88 \leqslant t \leqslant 1.00$ and the hexagonal $\mathrm{BaTiO}_{3}-$ type structure occurs in the range of $1.00 \leqslant t \leqslant 1.06$. On the other hand, $\mathrm{A}_{2} \mathrm{BF}_{4}$ crystals have the layered perovskite structure over the range of the tolerance factor corresponding to the cubic perovskite and hexagonal structure of $\mathrm{ABF}_{3}$ crystals. Crystals of $\mathrm{Tl}_{2} \mathrm{MgF}_{4}$ and $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ have the layered perovskite structure, in contrast with the hexagonal structure for $\mathrm{TlMgF}_{3}(t=1.03)$ and $\mathrm{TlZnF}_{3}(t=1.01)$ crystals [9]. Figure 1 shows the unit cell of layered perovskite $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ crystal, together with the cubic perovskite structure considered virtually. It must be emphasized that we can obtain the information on the charge-compensated centres formed in the virtual cubic perovskite crystal in figure 1(a) using the spin-Hamiltonian separation method, although the cubic perovskite structure does not occur in real $\mathrm{TlZnF}_{3}$ crystal.

Recently, we reported EPR results for tetragonal and orthorhombic centres observed in $\mathrm{Tl}_{2} \mathrm{MgF}_{4}$ and $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ crystals co-doped with $\mathrm{Cr}^{3+}$ and $\mathrm{Li}^{+}$[10]. It was found that the spectra of
tetragonal centres exhibit anomalously large fine-structure splittings, which were about double those in $\mathrm{K}_{2} \mathrm{MF}_{4}$ and $\mathrm{Rb}_{2} \mathrm{MF}_{4}(\mathrm{M}=\mathrm{Mg}, \mathrm{Zn})$. Using the spin-Hamiltonian separation analysis, the separated parameter corresponding to the uncompensated centre was in good agreement with the fine-structure parameter for the tetragonal centre. The tetragonal centre was identified unambiguously as the uncompensated centre in spite of the anomalously large fine-structure splittings. The orthorhombic centre was ascribed to a $\mathrm{Cr}^{3+}$ ion associated with a $\mathrm{Li}^{+}$ion at the nearest $\mathrm{Zn}^{2+}$ site (centre IV) [10].

In this paper, we will report EPR results for monoclinic (centre II) and orthorhombic (centre III) centres newly observed in $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ single crystals doped only with $\mathrm{Cr}^{3+}$. For identification of the centres II and III, the second-rank fine-structure terms will be analysed using the spin-Hamiltonian separation method. We will discuss the separated parameters by comparing with recent results for the centres I and IV in $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ and with those obtained from other perovskite crystals.

## 2. Experimental procedures and results

Single crystals of $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ were grown in graphite crucibles by the Bridgman technique. Powder of $\mathrm{CrF}_{3}$ was added to starting mixtures of $\mathrm{ZnF}_{2}$ and TIF. The crystals obtained are cleaved easily in the $c$-plane. The measurements were made at room temperature using a JESFE1XG ESR spectrometer operating in the X band at the Centre for Instrumental Analysis at Nagoya Institute of Technology.

For an as-grown crystal of $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ doped with $\mathrm{Cr}^{3+}$, signals from two kinds of new centre were observed at room temperature, together with those from the centre I previously reported [10]. A recorder trace of the EPR signals with $\boldsymbol{H} \| \boldsymbol{a}$ at room temperature is shown in figure 2(a). Figure 2(b) shows the recorder trace of the EPR signals obtained for another crystal co-doped with $\mathrm{Cr}^{3+}$ and $\mathrm{Li}^{+}$used for EPR observation in the previous work [10]. Signals from the centres I, II, III and IV are marked with Roman numerals in figure 2. The centres II and III disappear for the crystals co-doped with $\mathrm{Cr}^{3+}$ and $\mathrm{Li}^{+}$, as seen from figure 2(b). The centre IV is observed selectively in the $\mathrm{Li}^{+}$co-doped crystals.

In figure 3 signals observed at room temperature are plotted as open triangles for the centre I, open circles for the centre II and open squares for the centre III against the external field direction in the $c$-plane. The spectrum of the centre I show no variation in this plane. This indicates that the centre I has tetragonal symmetry about the crystalline $c$-axis.

The signals from the centre II have a set of branches, as seen in figure 3. The branches have peaks and troughs in the [110] field direction and coincide with each other in the [100] direction. From the field direction dependence in the (110) plane, we see that the signals from the centre II show extremes for a direction declined by about $36^{\circ}$ from the $c$-axis in the plane. This makes it clear that the spectra of the centre II have monoclinic symmetry. Each branch corresponds to the association of some charge compensator in one of the $\langle 110\rangle$ symmetry planes.

In contrast with those for the centre II, the branches for the centre III have peaks and troughs in the [100] direction and coincide with each other in the [110] direction as seen from figure 3. Another coincidence of the branches is observed in the [001] field direction. This makes it clear that the spectra of the centre III have orthorhombic symmetry due to some charge compensator along a crystalline axis in the $c$-plane. The disappearance of the centre III in $\mathrm{Li}^{+}$ co-doped crystals and the similarity of the field direction dependence to that of the centre IV indicate that the charge compensation for the centres III takes place at the same site as that of $\mathrm{Li}^{+}$for the centre IV.


Figure 2. Observed EPR spectra of the $\mathrm{Cr}^{3+}$ centres at room temperature with $\boldsymbol{H} \|$ [100] in $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ (a) doped only with $\mathrm{Cr}^{3+}$ and (b) co-doped with $\mathrm{Cr}^{3+}$ and $\mathrm{Li}^{+}$. The labels II and III denote respectively the signals from new monoclinic and orthorhombic centres. Signals from the centres I and IV previously reported [10] are denoted by I and IV.

The spectra of the centres II and III can be described by the following spin Hamiltonian:

$$
\begin{equation*}
\mathcal{H}=g_{z} \beta S_{z} B_{z}+g_{x} \beta S_{x} B_{x}+g_{y} \beta S_{y} B_{y}+\frac{1}{3}\left[b_{2}^{0} O_{2}^{0}+b_{2}^{2} O_{2}^{2}\right], \tag{1}
\end{equation*}
$$

where $O_{2}^{0}$ and $O_{2}^{2}$ are the Stevens operators defined by Abragam and Bleaney [11]. For the centre II, the spin Hamiltonian is described in the coordinate system where the $z$-axis is declined at an angle $\theta$ from the $c$-axis in the ( $\overline{1} 10)$ symmetry plane and the $x$-axis is in the same plane. For the centres III, the $z$-axis is chosen to be parallel to the $a$-axis where the spectrum shows maximum fine-structure splitting, and the $x$-axis is parallel to the $b$-axis.

Each spectrum observed was fitted to the spin Hamiltonian by the direct matrix diagonalization method. By this method, relative signs among $b_{2}^{m}$-parameters can be determined uniquely. The sign of $b_{2}^{0}$ for the centre II is selected to be negative as the value of $g_{z}-\left(g_{x}+g_{y}\right) / 2$ is negative. On the other hand, the signs of $b_{2}^{0}$ for the centres III and IV are selected to be positive as the values of $g_{z}-\left(g_{x}+g_{y}\right) / 2$ are positive, similarly to the cases for other layered perovskite fluorides [8]. The spin-Hamiltonian parameters obtained are listed in table 1 together with those obtained previously for the centres I and IV [10]. The sign of $\theta$ for the centre II cannot be determined by the matrix diagonalization method. It was determined by the spin-Hamiltonian separation analysis, to be mentioned in the following section. Dotted curves in figure 3 show the theoretical curves calculated using the spin-Hamiltonian parameters listed


Figure 3. Angular variation of the signals I, II and III labelled in figure 2(a) with $\boldsymbol{H}$ in the $c$-plane. Open circles are due to the centre II, open squares are due to the centre III and open triangles are due to the centre I. Dotted curves denote the resonance fields calculated using the parameters listed in table 1.

Table 1. Spin-Hamiltonian parameters for several kinds of $\mathrm{Cr}^{3+}$ centre observed in $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$. The positive sign of $\theta$ for the centre II is reasonable, as mentioned in section 4. The units are $10^{-4}$ $\mathrm{cm}^{-1}$ for $b_{0}^{2}$ and $b_{2}^{2}$.

| Centre | $g_{x}$ | $g_{y}$ | $g_{z}$ | $b_{2}^{0}$ | $b_{2}^{2}$ | $\theta(\mathrm{deg})$ |
| :--- | :--- | :--- | :--- | :---: | :---: | :---: |
| $\mathrm{I}^{10)}$ | $1.9724(6)$ | $1.9724(6)$ | $1.9715(6)$ | $-866.1(5)$ | - | - |
| II | $1.9810(5)$ | $1.9772(2)$ | $1.9629(6)$ | $-1507.9(8)$ | $-706.1(6)$ | $\pm 36.3(1)$ |
| III | $1.972(1)$ | $1.972(1)$ | $1.975(1)$ | $924.5(8)$ | $-156(1)$ | - |
| IV $^{10)}$ | $1.971(1)$ | $1.970(1)$ | $1.9734(8)$ | $684.6(7)$ | $529(1)$ | - |

in table 1. Good agreement of the calculated values of the resonant fields with experimental ones is obtained.

## 3. Spin-Hamiltonian separation analysis

The spin-Hamiltonian separation method has been successfully applied to identify the magnetic impurity centres in low-symmetry crystals [4-8]. For identification of charge-compensated centres in layered perovskite fluorides, the surroundings of the centres with lower symmetry can be interpreted by separating them into two configurations of surrounding ions. One is a similar configuration to that of the uncompensated centre in the same host crystal. The other is a configuration corresponding to the same kind of charge-compensated centre in the

Table 2. Values of $b_{2 a(1)}$ derived for the orthorhombic centres III, IV and values of $b_{2}^{0}$ for the centres I in several layered perovskite fluorides. The units are $10^{-4} \mathrm{~cm}^{-1}$ for the fine-structure parameters.

| Crystal | $a(\AA)$ | $c(\AA)$ | $b_{2}^{0}(\mathrm{I})$ | $b_{2 a(1)}(\mathrm{II})$ | $b_{2 a(1)}(\mathrm{III})$ | $b_{2 a(1)}(\mathrm{IV})$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{K}_{2} \mathrm{MgF}_{4}$ | 3.9704 | $13.176^{13)}$ | $-419^{4)}$ | -590.7 | $-443^{7)}$ | $-413.7^{7)}$ |
| $\mathrm{Tl}_{2} \mathrm{MgF}_{4}$ | 4.007 | $14.43^{9)}$ | $-1041.7^{10)}$ | - | - | $-1042.9^{10)}$ |
| $\mathrm{Rb}_{2} \mathrm{MgF}_{4}$ | 4.0584 | $13.7991^{13)}$ | $-526.1^{7)}$ | - | $-577.6^{7)}$ | $-564.0^{7)}$ |
| $\mathrm{K}_{2} \mathrm{ZnF}_{4}$ | 4.0548 | $13.096^{13)}$ | $-381^{4)}$ | -586.5 | $-402^{5)}$ | $-386^{5}$ |
| $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ | 4.105 | $14.10^{9)}$ | $-866.1^{10)}$ | -838.9 | -872.5 | $-860.9^{10)}$ |
| $\mathrm{Rb}_{2} \mathrm{ZnF}_{4}$ | 4.136 | $13.706^{13)}$ | $-369.0^{6)}$ | - | $-394.7^{6)}$ | $-410.8^{6)}$ |
| $\mathrm{K}_{2} \mathrm{CdF}_{4}$ | 4.3612 | $13.266^{13)}$ | $-643.1^{14)}$ | - | $-623.3^{14)}$ | - |
| $\mathrm{Rb}_{2} \mathrm{CdF}_{4}$ | 4.4017 | $13.938^{13)}$ | $-666.4^{6)}$ | - | $-665.4^{6)}$ | $-637.7^{6)}$ |
| $\mathrm{Cs}_{2} \mathrm{CdF}_{4}$ | - | - | $-702.0^{6)}$ | - | $-740.9^{6)}$ | $-733.4^{6)}$ |

cubic perovskite crystals composed of the same cations. The spectra of the centres II and III having lower symmetry than the tetragonal one in the same host crystal show that these centres are perturbed by some charge compensator nearby. The fine-structure parameters for the charge-compensated centres can be considered by separating the second-rank fine-structure terms into two uniaxial terms with the parameters $b_{2 a(1)}$ along the $c$-axis and $b_{2 a(2)}$ along the direction to the charge compensator. The separated axial parameters $b_{2 a(1)}$ are comparable with the parameter $b_{2}^{0}$ for the uncompensated centre in the same host crystal. The other axial parameter, $b_{2 a(2)}$, is compared with the parameter for the centre associated with the same kind of charge compensator in the cubic perovskite crystal.

For the monoclinic centre II the main principal axis (the $z$-axis) of the fine-structure terms is found to be declined by $36.3^{\circ}$ from the $c$-axis in the ( $\overline{1} 10$ ) plane, as shown in table 1 . The excess positive charge on the $\mathrm{Cr}^{3+}$ ion is assumed to be compensated locally by a vacancy at the nearest $\mathrm{Tl}^{+}$site along the [111] direction in this symmetry plane. So, we try to separate the fine-structure terms into two uniaxial terms as follows:

$$
\begin{equation*}
b_{2}^{0} O_{2}^{0}(z)+b_{2}^{2} O_{2}^{2}(x, y)=b_{2 a(1)} O_{2}^{0}\left(z^{\prime}\right)+b_{2 a(2)} O_{2}^{0}\left(z^{\prime \prime}\right) \tag{2}
\end{equation*}
$$

where the $z^{\prime}$-axis is parallel to the $c$-axis and the $z^{\prime \prime}$-axis is assumed to be declined by $54.7^{\circ}$ from the $c$-axis in the ( $\overline{1} 10$ ) plane. Using the transformation properties of the Stevens operators given by Rudowicz [12], we can deduce the following conditions that satisfy equation (2):

$$
\begin{align*}
& b_{2 a(1)}=\frac{1}{2}\left(3 \cos ^{2} \theta-1\right) b_{2}^{0}+\frac{1}{2} \sin ^{2} \theta b_{2}^{2},  \tag{3}\\
& b_{2 a(2)}=\frac{3}{2} \sin ^{2} \theta b_{2}^{0}+\frac{1}{2}\left(\cos ^{2} \theta+1\right) b_{2}^{2} \tag{4}
\end{align*}
$$

and

$$
\begin{equation*}
\sin 2 \theta=\frac{2 \sqrt{2} b_{2 a(2)}}{3 b_{2}^{0}-b_{2}^{2}} \tag{5}
\end{equation*}
$$

We can calculate the separated axial parameters $b_{2 a(1)}$ and $b_{2 a(2)}$ from equations (3) and (4) using the experimental values of $b_{2}^{0}, b_{2}^{2}$ and $\theta$ listed in table 1 . The values obtained are tabulated in tables 2 and 3. The sign of the angle $\theta$ is determined as positive from equation (5). The negative value of $b_{2 a(2)}$ is consistent with the positive sign of $\theta$, since $3 b_{2}^{0}-b_{2}^{2}<0$ as seen from table 1 .

We also analyse the orthorhombic centres III using the spin-Hamiltonian separation method. We separate the second-rank fine-structure terms into a uniaxial term with the parameters $b_{2 a(1)}$ along the crystalline $c$-axis (the $y$-axis) and a uniaxial term with $b_{2 a(2)}$

Table 3. Values of $b_{2 a(2)}$ derived for the monoclinic centres II in several layered perovskite fluorides. The fourth column gives the values of $b_{2}^{0}$ for the trigonal $\mathrm{Cr}^{3+}-\mathrm{V}_{\mathrm{K}}$ centres in the corresponding cubic perovskite fluorides. The units are $10^{-4} \mathrm{~cm}^{-1}$.

| Crystal | $b_{2 a(2)}$ | Crystal | $b_{2}^{0}$ | Reference |
| :--- | :---: | :--- | :---: | :--- |
| $\mathrm{K}_{2} \mathrm{MgF}_{4}$ | -1411.3 | $\mathrm{KMgF}_{3}$ | -1528 | $[2]$ |
| $\mathrm{K}_{2} \mathrm{ZnF}_{4}$ | -1573.5 | $\mathrm{KZnF}_{3}$ | -1613 | $[2]$ |
| $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ | -1375.1 | $\mathrm{TlZnF}_{3}$ | - | This work |

Table 4. Values of $b_{2 a(2)}$ derived for the orthorhombic centres III and IV in the layered perovskite fluorides $\mathrm{A}_{2} \mathrm{MF}_{4}$. The $\Delta b_{2 a}$ column gives the values of the difference $b_{2 a(2)}(\mathrm{III})-b_{2 a(2)}(\mathrm{IV})$. The units are $10^{-4} \mathrm{~cm}^{-1}$.

| $\mathrm{A}_{2} \mathrm{MF}_{4}$ | $b_{2 a(2)}(\mathrm{III})$ | $b_{2 a(2)}(\mathrm{IV})$ | $\Delta b_{2 a}$ |
| :--- | :--- | :--- | :---: |
| $\mathrm{~K}_{2} \mathrm{MgF}_{4}$ | $-565^{7)}$ | $-470.3^{7)}$ | -94.7 |
| $\mathrm{Tl}_{2} \mathrm{MgF}_{4}$ | - | $-644.3^{10)}$ | - |
| $\mathrm{Rb}_{2} \mathrm{MgF}_{4}$ | $-583.8^{7)}$ | $-610.2^{7)}$ | +26.4 |
| $\mathrm{~K}_{2} \mathrm{ZnF}_{4}$ | $-424^{5)}$ | $-374^{5)}$ | -50 |
| $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ | -976.5 | $-508.3^{10)}$ | -468.2 |
| $\mathrm{Rb}_{2} \mathrm{ZnF}_{4}$ | $-408.3^{6)}$ | $-455.4^{6)}$ | +47.1 |
| $\mathrm{~K}_{2} \mathrm{CdF}_{4}$ | $-346.9^{14)}$ | - | - |
| $\mathrm{Rb}_{2} \mathrm{CdF}_{4}$ | $-442.6^{6)}$ | $-584.7^{6)}$ | +142.1 |
| $\mathrm{Cs}_{2} \mathrm{CdF}_{4}$ | $-503.1^{6)}$ | $-710.8^{6)}$ | +207.7 |

along the crystalline $b$-axis (the $x$-axis) in the $c$-plane. The fine-structure terms in the $x, y, z$ coordinate system can be written as follows:

$$
\begin{equation*}
b_{2}^{0} O_{2}^{0}(z)+b_{2}^{2} O_{2}^{2}(x, y)=b_{2 a(1)} O_{2}^{0}(y)+b_{2 a(2)} O_{2}^{0}(x) \tag{6}
\end{equation*}
$$

The term $b_{2 a(1)} O_{2}^{0}(y)$ denotes the uniaxial term, about the $y$-axis, where $O_{2}^{0}(y)=3 S_{y}^{2}-S(S+$ 1). Equation (6) is valid when the following conditions are satisfied:

$$
\begin{equation*}
b_{2 a(1)}=-b_{2}^{0}-\frac{1}{3} b_{2}^{2}, \quad b_{2 a(2)}=-b_{2}^{0}+\frac{1}{3} b_{2}^{2} . \tag{7}
\end{equation*}
$$

Values of the separated axial parameters $b_{2 a(1)}$ and $b_{2 a(2)}$ calculated from the experimental values of $b_{2}^{0}$ and $b_{2}^{2}$ listed in table 1 are tabulated in tables 2 and 4 .

## 4. Discussion

### 4.1. Centre I

The signals from the centre I with tetragonal symmetry were observed with large intensity for both crystals doped with $\mathrm{Cr}^{3+}$ and co-doped with $\mathrm{Cr}^{3+}$ and $\mathrm{Li}^{+}$as shown in figure 2. In table 2 the separated parameters $b_{2 a(1)}$ obtained from the centres II, III and IV in $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ are listed together with those for other layered perovskite fluorides reported previously [4, 5, 7, 13]. The fine-structure parameters $b_{2}^{0}$ for the centres I are also listed in this table for comparison. All separated parameters $b_{2 a(1)}$ for the centres II, III and IV in $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ have values close to the $b_{2}^{0}$-parameter for the centre I in the same host crystal. The result indicates that the separations for the centres II and III made in section 3 are appropriate. This makes it possible to consider the parameter $b_{2 a(2)}$ as the information on $b_{2}^{0}$ for the same kind of charge-compensated centre in the virtual cubic perovskite $\mathrm{Tl}_{\mathrm{ZnF}}^{3}$ crystal, although the real structure of $\mathrm{TlZnF}_{3}$ is hexagonal. It may be safely said that the centre I is ascribable to a $\mathrm{Cr}^{3+}$ ion substituted for the $\mathrm{Zn}^{2+}$ site

(a)

(b)

(c)

Figure 4. Schematic models for (a) the centre I, (b) the centre II and (c) the centre III.
without any charge compensator in its immediate neighbourhood. A schematic model for the centre $I$ is shown in figure 4(a).

The magnitude of the parameter $b_{2}^{0}$ for the centre I for $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ is about double that for $\mathrm{Rb}_{2} \mathrm{ZnF}_{4}$. This tendency also holds between $\mathrm{Tl}_{2} \mathrm{MgF}_{4}$ and $\mathrm{Rb}_{2} \mathrm{MgF}_{4}$ crystals. The lattice parameters $a$ are almost the same for the two crystals. The difference in $b_{2}^{0}$-parameters comes from the difference in monovalent cations of the host crystals. As seen from table 2, the lattice parameters $c$ for $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ and $\mathrm{Tl}_{2} \mathrm{MgF}_{4}$ are larger than those for $\mathrm{Rb}_{2} \mathrm{ZnF}_{4}$ and $\mathrm{Rb}_{2} \mathrm{MgF}_{4}$ although the ionic radius ( $1.47 \AA$ ) of $\mathrm{Tl}^{+}$is the same as that of $\mathrm{Rb}^{+}$. The effect of $\mathrm{Tl}^{+}$ions on the local environment around the $\mathrm{Cr}^{3+}$ ion may be related to the difference in lattice parameter $c$.

### 4.2. Centre II

The parameters $b_{2 a(2)}$ derived from the centre II are listed in table 3 together with those derived from the monoclinic centres reported in the layered perovskite fluorides $K_{2} M F_{4}(\mathrm{M}=\mathrm{Mg}$, Zn ) [4]. The $b_{2}^{0}$ for the trigonal $\mathrm{Cr}^{3+}-\mathrm{V}_{\mathrm{K}}$ centres in the cubic perovskite crystals $\mathrm{KMF}_{3}$ [2] are also listed for comparison. The value of $b_{2 a(2)}$ for $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ is close to $b_{2 a(2)}$ for $\mathrm{K}_{2} \mathrm{MF}_{4}$ and to $b_{2}^{0}$ for the $\mathrm{Cr}^{3+}-\mathrm{V}_{\mathrm{K}}$ centres in $\mathrm{KMF}_{3}$. This shows that the centre II in $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ can be considered to be associated with the same kind of charge compensator as those in other crystals. So, the centre II can be ascribed to a $\mathrm{Cr}^{3+}$ ion at the $\mathrm{Zn}^{2+}$ site associated with a vacancy at the nearest $\mathrm{Tl}^{+}$site, as shown in figure 4(b).

It must be emphasized that the relationship between the direction of the principal $z$-axis in the spin Hamiltonian and the configuration of the centre with charge compensator can be clarified by spin-Hamiltonian separation analysis. As mentioned in section 3, the sign of the angle $\theta$ in table 1 is determined as positive. This shows that the direction of the $z$-axis for the centre II is declined from the [001] axis by an angle of about $36^{\circ}$ in the ( $\overline{1} 10$ ) plane toward the same direction to the vacancy at the nearest $\mathrm{Tl}^{+}$site.

### 4.3. Centre III

The orthorhombic centres observed in several layered perovskite fluorides have been identified using the spin-Hamiltonian separation analysis [4, 5, 7, 12], where the excess positive charge

Table 5. Values of $b_{2}^{0}$ for the $\mathrm{Cr}^{3+}-\mathrm{V}_{\mathrm{M}}$ and the $\mathrm{Cr}^{3+}-\mathrm{Li}^{+}$centres in cubic perovskite fluorides $\mathrm{AMF}_{3}$. The $\Delta b_{2}^{0}$ column gives the values of the difference $b_{2}^{0}\left(\mathrm{~V}_{\mathrm{M}}\right)-b_{2}^{0}(\mathrm{Li})$. Asterisks denote $\mathrm{TlMgF}_{3}, \mathrm{TlZnF}_{3}$ and $\mathrm{RbMgF}_{3}$ having not cubic perovskite structures but hexagonal ones. The units are $10^{-4} \mathrm{~cm}^{-1}$.

| $\mathrm{AMF}_{3}$ | $b_{2}^{0}\left(\mathrm{~V}_{\mathrm{M}}\right)$ | $b_{2}^{0}\left(\mathrm{Li}^{+}\right)$ | $\Delta b_{2}^{0}$ |
| :--- | :---: | :---: | :--- |
| $\mathrm{KMgF}_{3}$ | - | - | - |
| $\mathrm{TlMgF}_{3}^{*}$ | - | - | - |
| $\mathrm{RbMgF}_{3}^{*}$ | - | - | - |
| $\mathrm{KZnF}_{3}$ | $-542.1^{3)}$ | $-508.0^{3)}$ | -34.1 |
| $\mathrm{TlZnF}_{3}^{*}$ | - | - | - |
| $\mathrm{RbZnF}_{3}$ | $-535^{6)}$ | $-594.4^{6)}$ | +59.4 |
| $\mathrm{KCdF}_{3}$ | $-511.3^{3)}$ | $-621.2^{3)}$ | +109.9 |
| $\mathrm{RbCdF}_{3}$ | $-569.3^{3)}$ | $-743.9^{3)}$ | +174.6 |
| $\mathrm{CsCdF}_{3}$ | $-629.3^{3)}$ | $-858.8^{3)}$ | +229.5 |

on the $\mathrm{Cr}^{3+}$ at a divalent cation site is compensated by a vacancy (centre III) or $\mathrm{Li}^{+}$(centre IV) at the nearest divalent cation site. As shown in table 4, the separated parameters $b_{2 a(2)}$ for the centres III and IV in $\mathrm{A}_{2} \mathrm{MF}_{4}$ are compared with the parameters $b_{2}^{0}$ for the $\mathrm{Cr}^{3+}-\mathrm{V}_{\mathrm{M}}$ and $\mathrm{Cr}^{3+}-\mathrm{Li}^{+}$centres. As $\mathrm{TlZnF}_{3}$ has not the cubic perovskite structure but the hexagonal one, the separated parameters $b_{2 a(2)}$ for the centres III and IV in $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ give additional information on the parameter $b_{2}^{0}$ for the centres formed virtually in the cubic perovskite structure.

The value of $b_{2 a(2)}$ for the centre IV in $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ is close to $b_{2 a(2)}$ for the centres IV in other crystals, as seen from table 4 . So, the centre IV in $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ can be ascribed to a $\mathrm{Cr}^{3+}$ ion associated with a $\mathrm{Li}^{+}$ion at the nearest $\mathrm{Zn}^{2+}$ site for compensation of excess positive charge on a $\mathrm{Cr}^{3+}$ at the $\mathrm{Zn}^{2+}$ site [4]. As mentioned in section 3, the charge compensation in the centres III and IV takes place at the same site in this crystal. The centre III can be ascribed to a $\mathrm{Cr}^{3+}$ ion associated with a vacancy at the nearest $\mathrm{Zn}^{2+}$ site in the $c$-plane, as shown in figure 4(c).

The negative sign of $b_{2}^{0}$ for the centre I in table 2 arises from the deviation of the apical ligand $\mathrm{F}^{-}$ions on the $c$-axis toward the $\mathrm{Cr}^{3+}$ ion, resulting in a compressed ligand octahedron along the $c$-axis. The magnitudes of the parameter $b_{2 a(2)}$ derived for the centres IV in the layered perovskite fluoride are slightly smaller than those of the parameter $b_{2}^{0}$ for the corresponding centres in the perovskite fluorides, as seen from tables 4 and 5. Smaller $\left|b_{2 a(2)}\right|$ values suggest that two apical ligand $\mathrm{F}^{-}$ions on the $c$-axis prevent the deviation of the intervening $\mathrm{F}^{-}$ion between the $\mathrm{Cr}^{3+}$ and $\mathrm{Li}^{+}$ions toward the $\mathrm{Cr}^{3+}$ ion by $\mathrm{F}^{-}-\mathrm{F}^{-}$Coulomb repulsion.

The dependence of the difference $\Delta b_{2 a(2)}\left(=b_{2 a(2)}(\mathrm{III})-b_{2 a(2)}(\mathrm{IV})\right)$ on the metal-ligand distance in the $c$-plane is shown in figure 5. A similar dependence of the difference $\Delta b_{2}^{0}$ $\left(=b_{2}^{0}\left(\mathrm{~V}_{\mathrm{M}}\right)-b_{2}^{0}(\mathrm{Li})\right)$ for cubic perovskite fluorides is also shown in the figure. The dependence of $\Delta b_{2 a(2)}$ on M-F distance is similar to that of $\Delta b_{2}^{0}$ except for $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$, as seen from figure 5 . For $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ the value of the difference $\Delta b_{2 a(2)}$ has negative sign and has an anomalously large magnitude. This result arises from $b_{2 a(2)}$ for the centre III in $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ having an anomalously large magnitude in contrast with that for the centre IV, as seen from table 4. The magnitude of $b_{2 a(2)}$ for the centre III is about double those of $\mathrm{Rb}_{2} \mathrm{ZnF}_{4}$ and $\mathrm{K}_{2} \mathrm{ZnF}_{4}$, similarly to the case for $b_{2}^{0}$ for the centre I.

The anomaly of $b_{2}^{0}$ for the centre I may arise from some effect on the local distortion of the apical ligand $\mathrm{F}^{-}$ions by the nearest $\mathrm{Tl}^{+}$ions along the $\langle 111\rangle$ axes and the next-nearest $\mathrm{Tl}^{+}$ions along the $c$-axis. The anomalously large magnitude of $b_{2 a(2)}$ for the centre III may arise from some effect of the nearest $\mathrm{Tl}^{+}$ions on the local distortion of the intervening $\mathrm{F}^{-}$ion between the $\mathrm{Cr}^{3+}$ ion and the vacancy at the nearest $\mathrm{Zn}^{2+}$ site. The value of $b_{2 a(2)}$ for the centre


Figure 5. Dependences of $\Delta b_{2 a(2)}$ and $\Delta b_{2}^{0}$ on the metal-ligand distance in the $c$-plane. Open circles show $\Delta b_{2 a(2)}=\left(b_{2 a(2)}(\mathrm{III})-b_{2 a(2)}\right.$ (IV)) for layered perovskite fluorides. Closed circles show $\Delta b_{2}^{0}=\left(b_{2}^{0}\left(\mathrm{~V}_{\mathrm{M}}\right)-b_{2}^{0}(\mathrm{Li})\right)$ for cubic perovskite fluorides.

II with a vacancy at the nearest $\mathrm{Tl}^{+}$site shows no anomaly, as seen from table 3 . We conclude that the anomaly for the centres I and III may arise from some effect of monovalent $\mathrm{Tl}^{+}$ions nearby. The anomaly in $b_{2 a(2)}$ for the centre III suggests that a similar effect of $\mathrm{Tl}^{+}$ions may take place in $b_{2}^{0}$ for the $\mathrm{Cr}^{3+}-\mathrm{V}_{\mathrm{M}}$ centres in cubic perovskite $\mathrm{TlMF}_{3}$.

## 5. Conclusions

Three kinds of EPR spectrum for the $\mathrm{Cr}^{3+}$ centres (I, II, III) have been observed for $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ crystals doped with $\mathrm{Cr}^{3+}$. One comprises the signals from the tetragonal $\mathrm{Cr}^{3+}$ centre (I) with strong intensity and the others comprise those from the monoclinic (II) and the orthorhombic (III) centres. For the centres II and III the fine-structure parameters are considered using spin-Hamiltonian separation analysis. The separated parameters $b_{2 a(1)}$ for centres II and III have values close to the parameter $b_{2}^{0}$ for the centre I. The monoclinic centre II is ascribed to a $\mathrm{Cr}^{3+}$ ion associated with the nearest $\mathrm{Tl}^{+}$vacancy (the $\mathrm{Cr}^{3+}-\mathrm{V}_{\mathrm{Tl}}$ centre). The orthorhombic centre III is ascribed to a $\mathrm{Cr}^{3+}$ ion associated with the nearest $\mathrm{Zn}^{2+}$ vacancy in the $c$-plane (the $\mathrm{Cr}^{3+}-\mathrm{V}_{\mathrm{Zn}}$ centre) .

Anomalies are found in $b_{2}^{0}$ for the centre I , in the separated parameters $b_{2 a(1)}$ for the centres II and III and in $b_{2 a(2)}$ for the centre III. The fine-structure parameters have at least double the magnitude of those for $\mathrm{Rb}_{2} \mathrm{ZnF}_{4}$ and $\mathrm{K}_{2} \mathrm{ZnF}_{4}$. The value of $b_{2 a(2)}$ for the centre II with a vacancy at the nearest $\mathrm{Tl}^{+}$site shows no anomaly compared with those for the same kind of the centre in cubic and layered perovskite fluorides. The anomaly of $b_{2}^{0}$ for the centre I may arise from some effects of the nearest and the next-nearest $\mathrm{Tl}^{+}$ions on the distortion of apical ligand $\mathrm{F}^{-}$ions along the $c$-axis. The anomaly of $b_{2 a(2)}$ for the centre III may arise from some effect of the nearest $\mathrm{Tl}^{+}$ions on the distortion of the intervening $\mathrm{F}^{-}$ion between $\mathrm{The}^{\mathrm{Cr}^{3+}}$ and the vacancy at the nearest $\mathrm{Zn}^{2+}$ site.

The parameters $b_{2 a(2)}$ for $\mathrm{Tl}_{2} \mathrm{ZnF}_{4}$ can be considered as information on $b_{2}^{0}$ for the same kind of centre formed in virtual cubic $\mathrm{TlZnF}_{3}$ crystal, although the real crystal of $\mathrm{TlZnF}_{3}$ has the hexagonal structure. The anomaly of $b_{2 a(2)}$ for the centre III suggests that the effect of the $\mathrm{Tl}^{+}$ions is on $b_{2}^{0}$ for the $\mathrm{Cr}^{3+}-\mathrm{V}_{\mathrm{M}}$ centres in cubic perovskite $\mathrm{TlMF}_{3}$. $\mathrm{The}^{\mathrm{Tl}}{ }^{+}$ions in the
crystals may cause local distortions around the $\mathrm{Cr}^{3+}$ ion different from those in the crystals with other monovalent cations such as $\mathrm{Rb}^{+}, \mathrm{K}^{+}$and $\mathrm{Cs}^{+}$.

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